

# Зеркальное Андреевское отражение

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# План лекции

- *Андреевское отражение*
- *Металл, диэлектрик, полуметалл*
- *Зеркальное Андреевское отражение на границе между сверхпроводником и двумерным полуметаллом.*
- *Полуметалл Вейля*

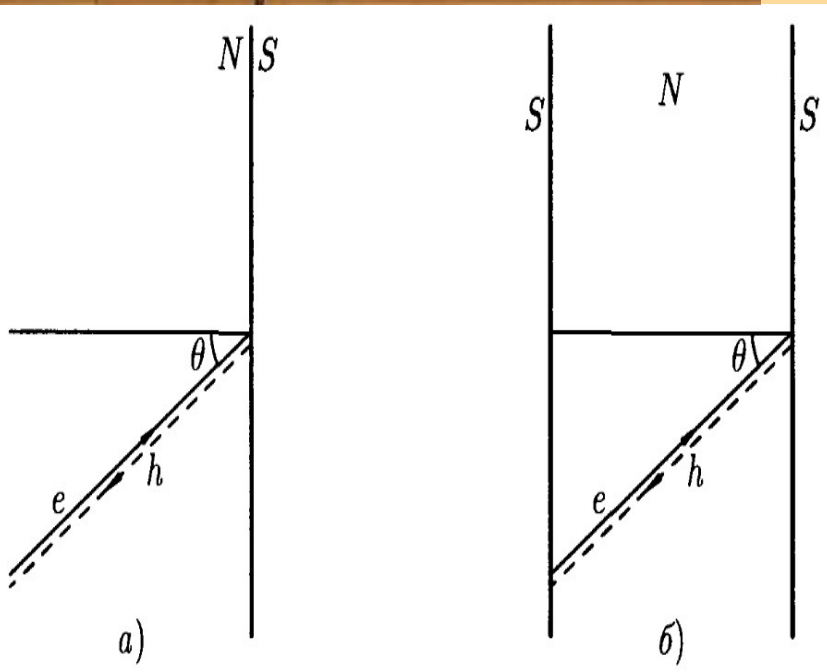
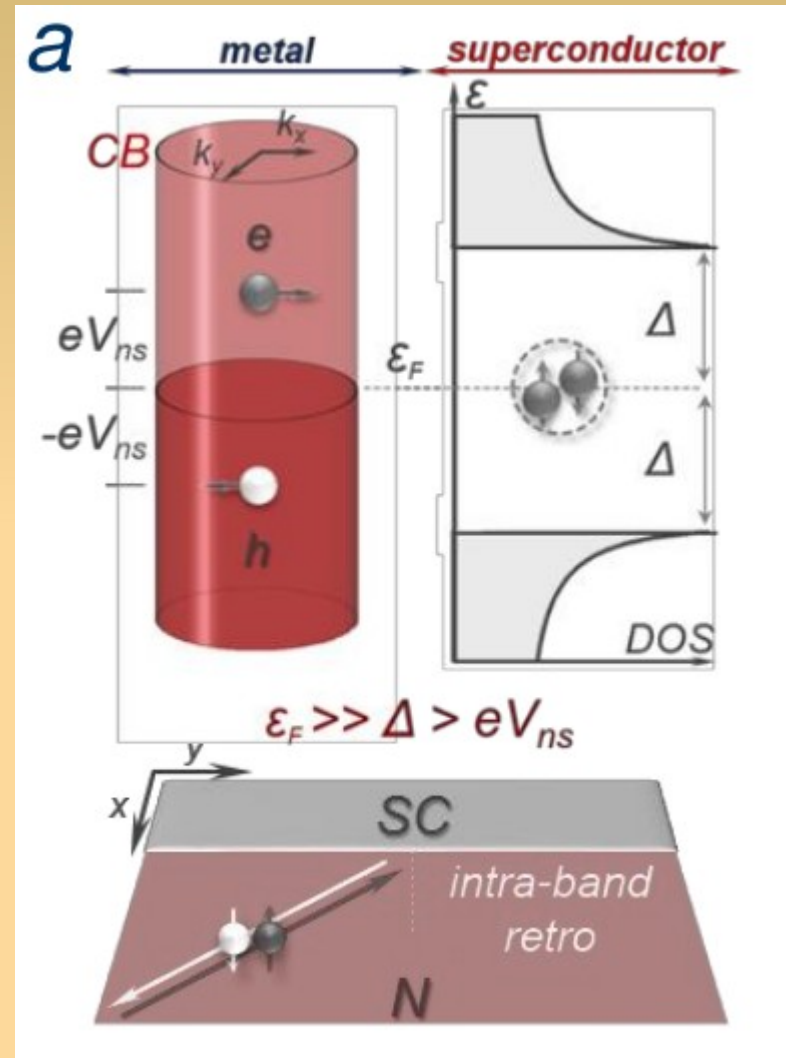
# Фундаментальные результаты физики твёрдого тела

**XX век - макроскопические квантовые эффекты**

- *Сверхпроводимость*
- *Физика низкоразмерных систем (квантовый эффект Холла)*

**XXI век - топологические эффекты**

# Андреевское отражение

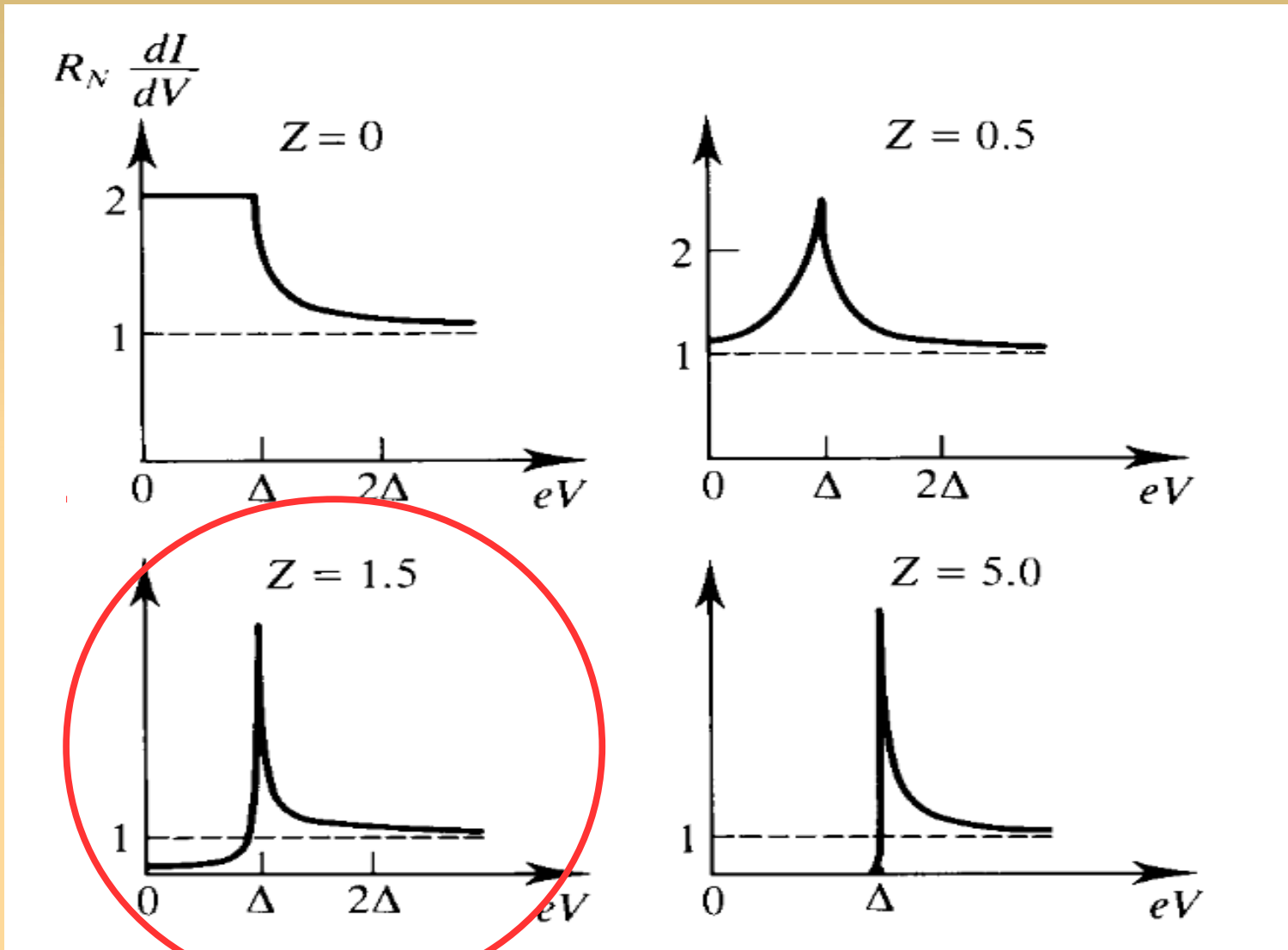


D. K. Efetov, L. Wang, C. Handschin, K. B. Efetov, J. Shuang, R. Cava, T. Taniguchi, K. Watanabe, J. Hone, C. R. Dean, P. Kim, *Nature Physics* (2015)

# SN contact: Andreev reflection (BTK)



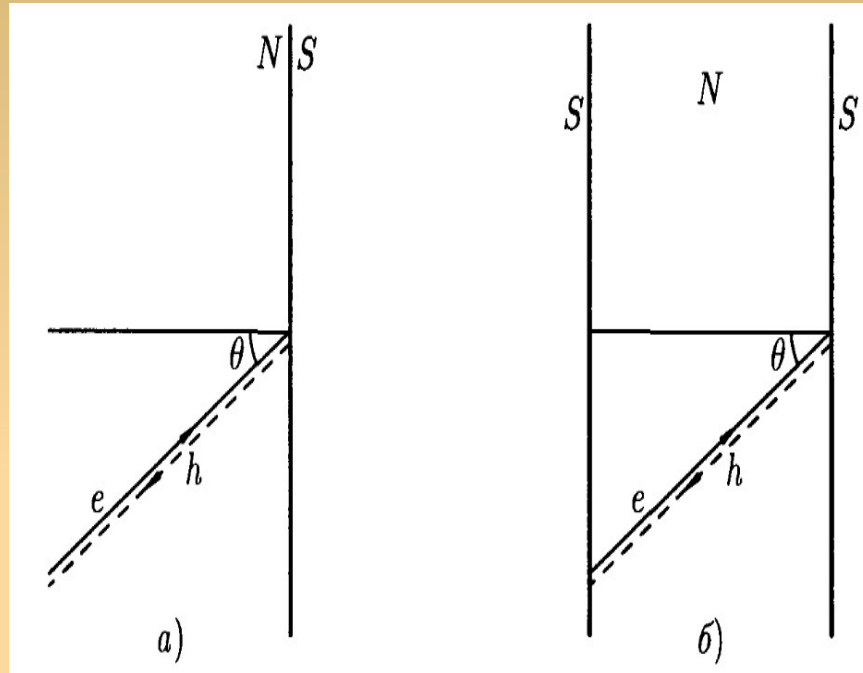
Teun Klapwijk



BTK (G.E. Blonder, M. Tinkham, T.M. Klapwijk, *Physical Review B*. 25, 4515, (1982))

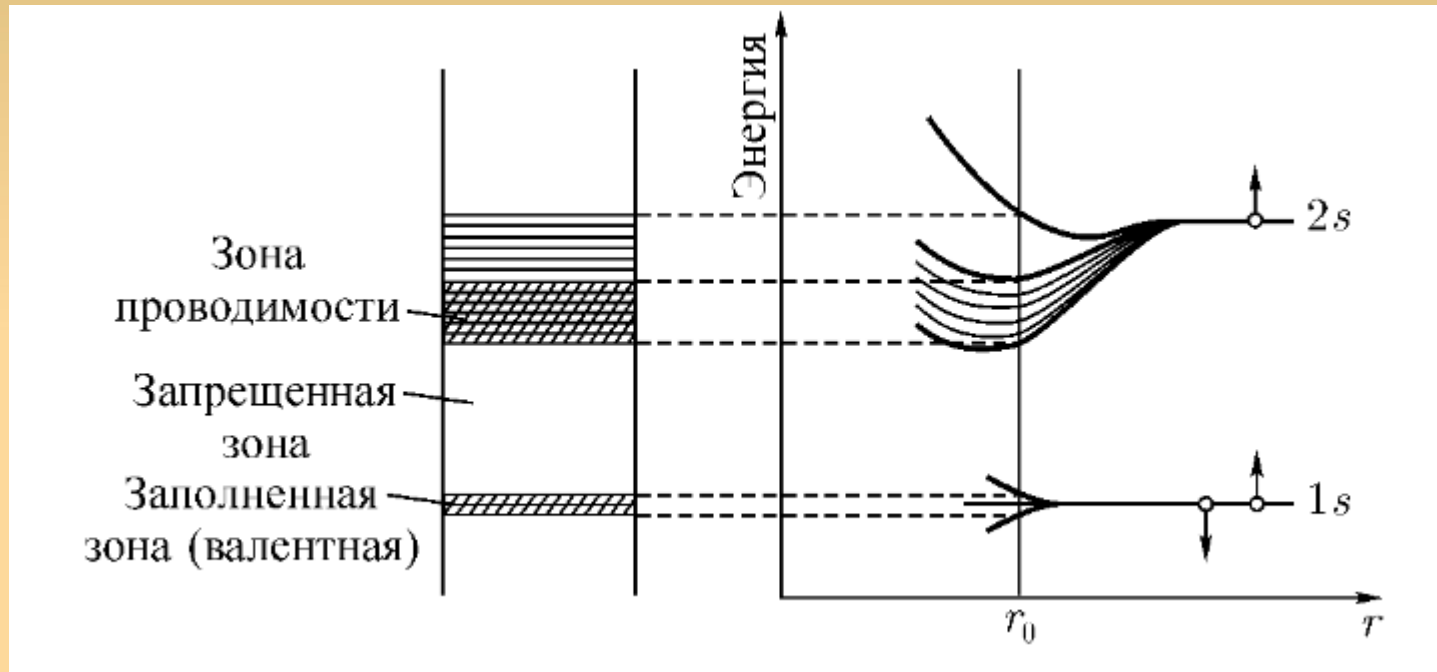
M. Tinkham, *Introduction to Superconductivity* (2d ed., McGrawHill, New York, 1996).

# Дырки бывают разные...



*О каких дырках мы говорим?*

# Электрон в периодическом потенциале. Зонная структура



Дж. Займан, Принципы теории твердого тела, учебник

# Заполнение квантовых состояний.

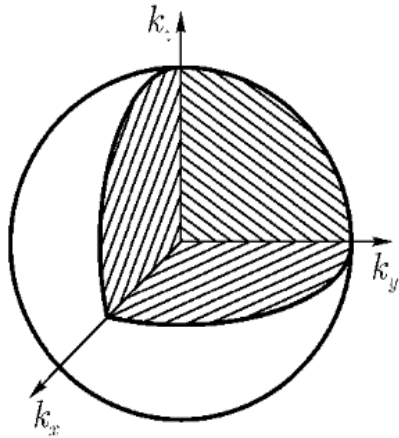


Рис. 82. К расчету числа состояний. Сфера в пространстве волновых чисел.

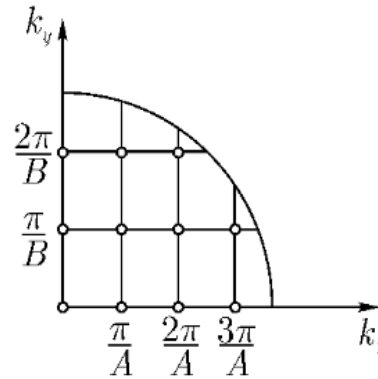
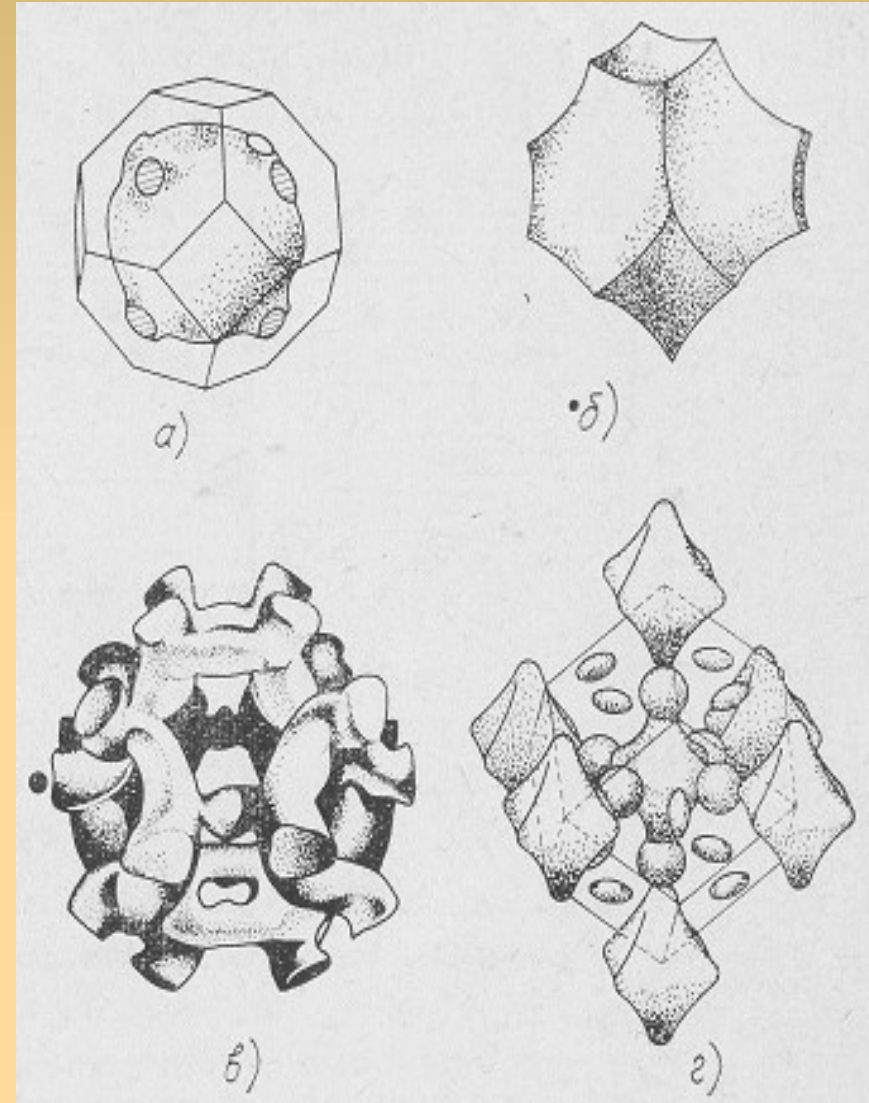


Рис. 83. К расчету числа состояний. «Разрешенные точки» на плоскости волновых чисел.





# Металл, диэлектрик, полупроводник. Зонная структура



**Металл – зона проводимости частично заполнена**

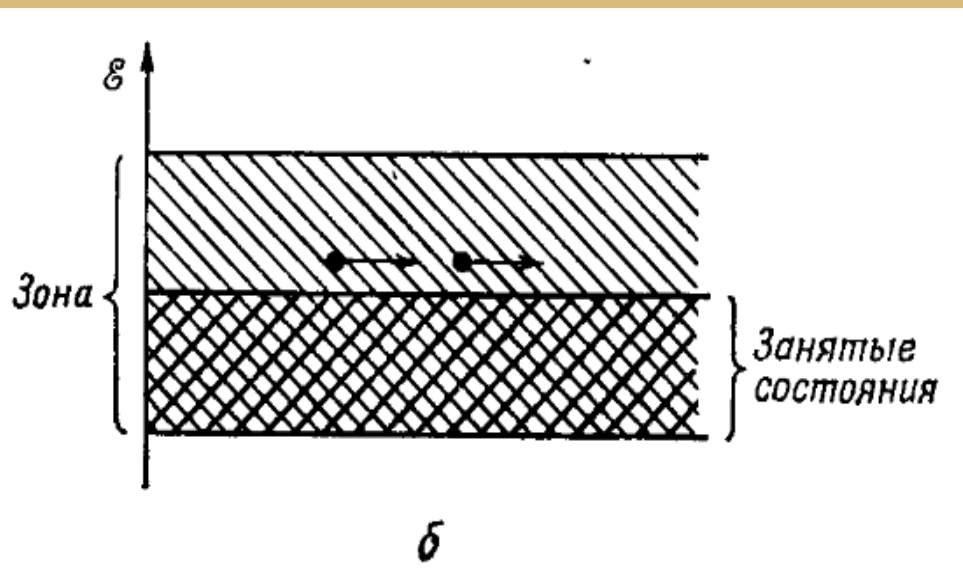
**Диэлектрик – зона проводимости пуста, валентная зона заполнена полностью**

**Полупроводник – диэлектрик, у которого ширина запрещённой зоны сравнима с температурой эксперимента (появление активационной проводимости)**

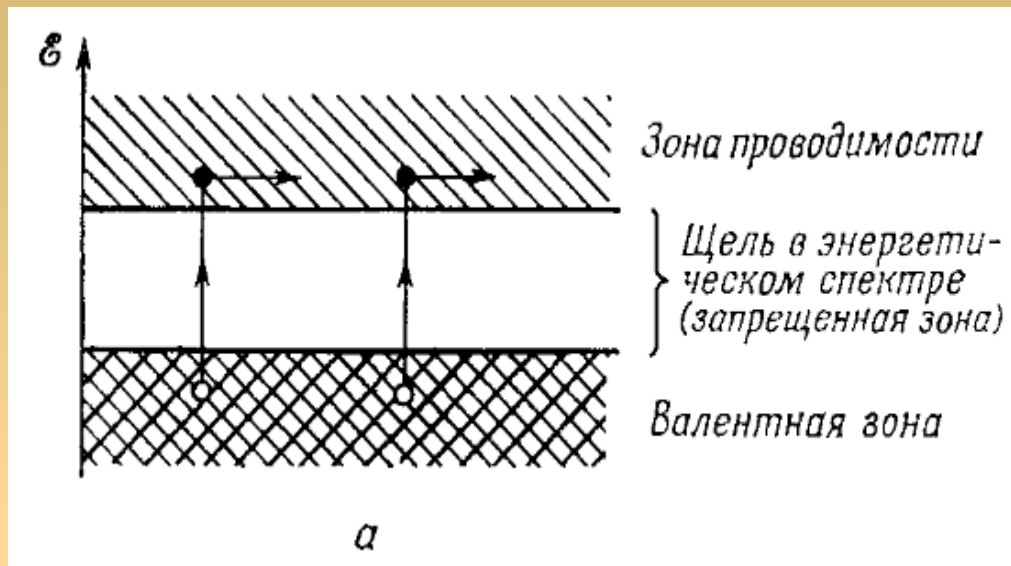
# Электронны и дырки

- *Дырки в зоне проводимости*
- *Дырки в валентной зоне*

# Электроны и дырки

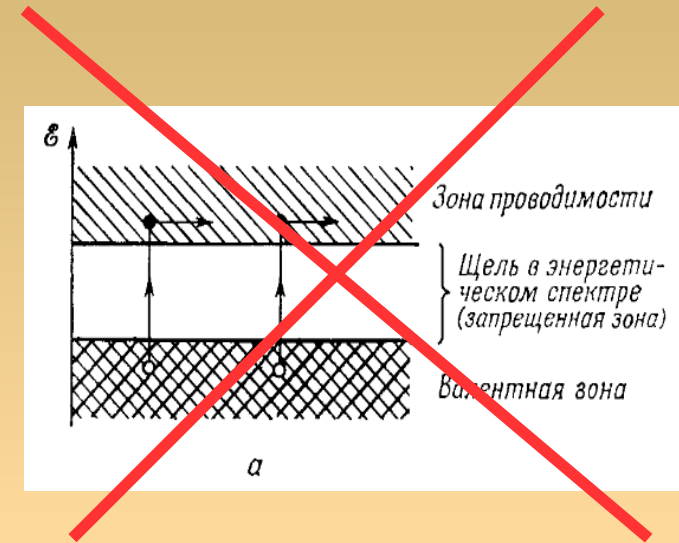
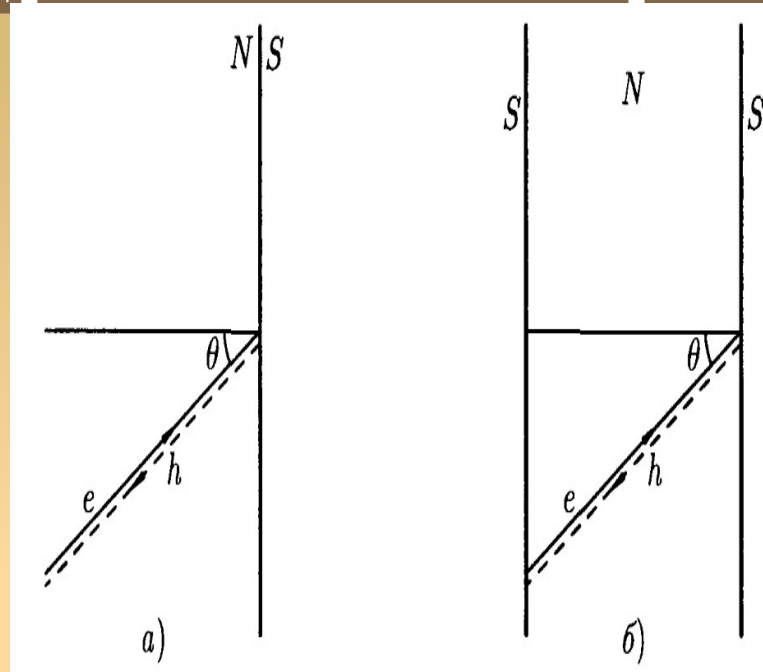
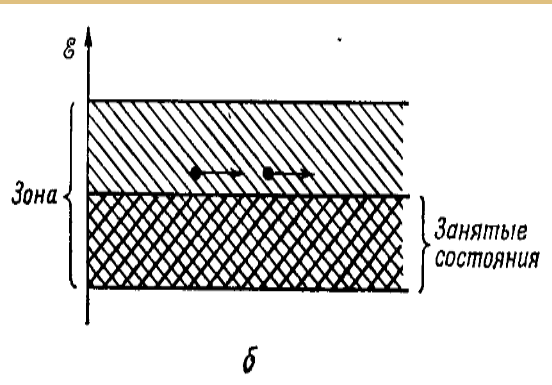


The metal-like hole remains in the conduction band of the normal metal, and therefore necessarily carries the opposite sign of the mass as compared to the electron.



The semiconductor-like hole now has the same mass sign as the electron

# Ретро (обычное) Андреевское отражение



For a straight N/SC interface, the momentum conservation along the boundary must be conserved.

Thus the incidence angle of an incoming electron,  $\theta_{\text{inc}}$ , and the reflected angle of a hole,  $\theta_{\text{ref}}$ , have a simple relation  $p_e \sin \theta_{\text{inc}} = p_h \sin \theta_{\text{ref}}$ , where  $p_e$  and  $p_h$  are the total momentum of the electron and hole, respectively.

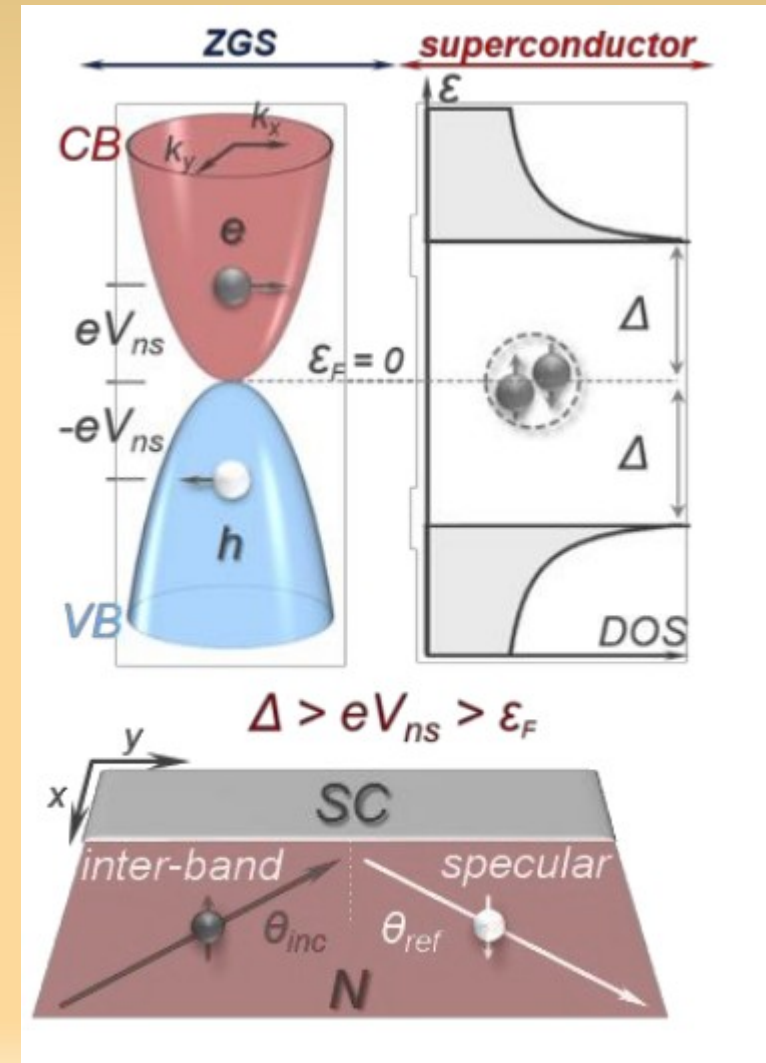
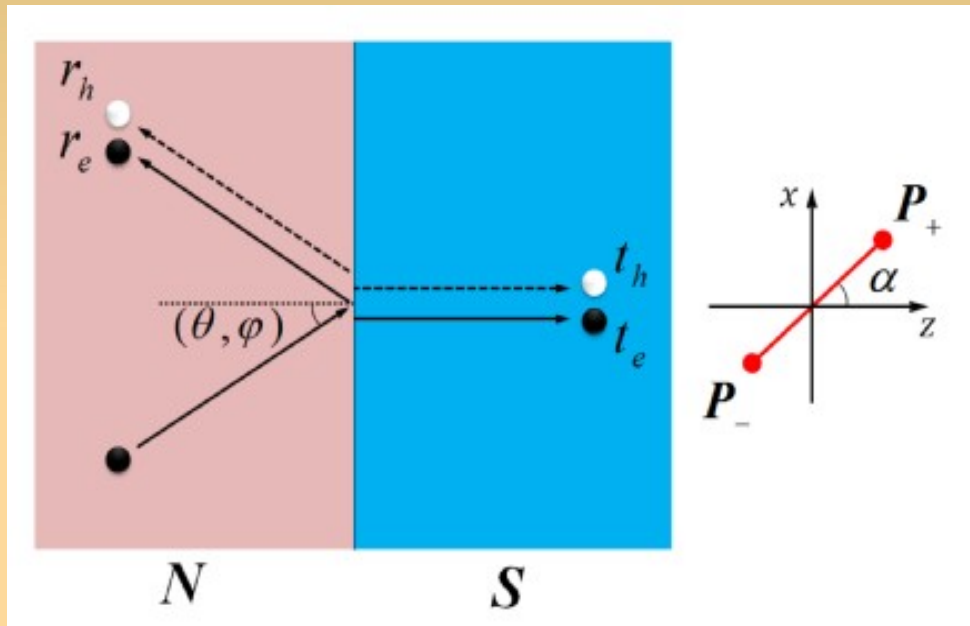
**In the limit  $\epsilon_F \gg \Delta$ , which holds for a typical NS junction**, the reflected hole is metal-like and remains in the conduction band of the normal metal, and therefore necessarily carries the opposite sign of the mass as compared to the electron.

To conserve the momentum, the hole reflects back along a path of the incident electron, exhibiting nearly perfect retro-AR, with  $\theta_{\text{ref}} \approx -\theta_{\text{inc}}$

# Спекулярное (зеркальное) Андреевское отражение

C. W. J. Beenakker, Physical Review Letters 97 (2006).

C. W. J. Beenakker, Reviews of Modern Physics 80, 1337 (2008).



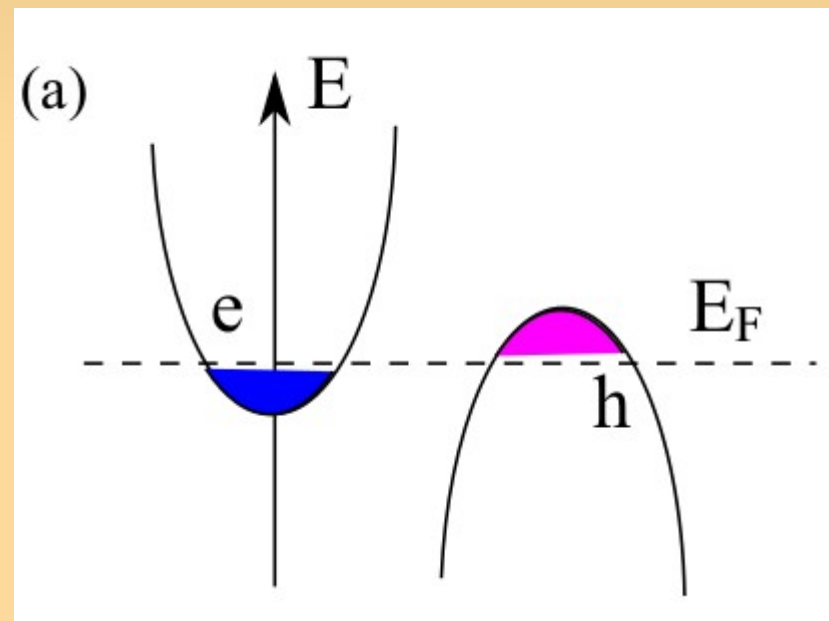
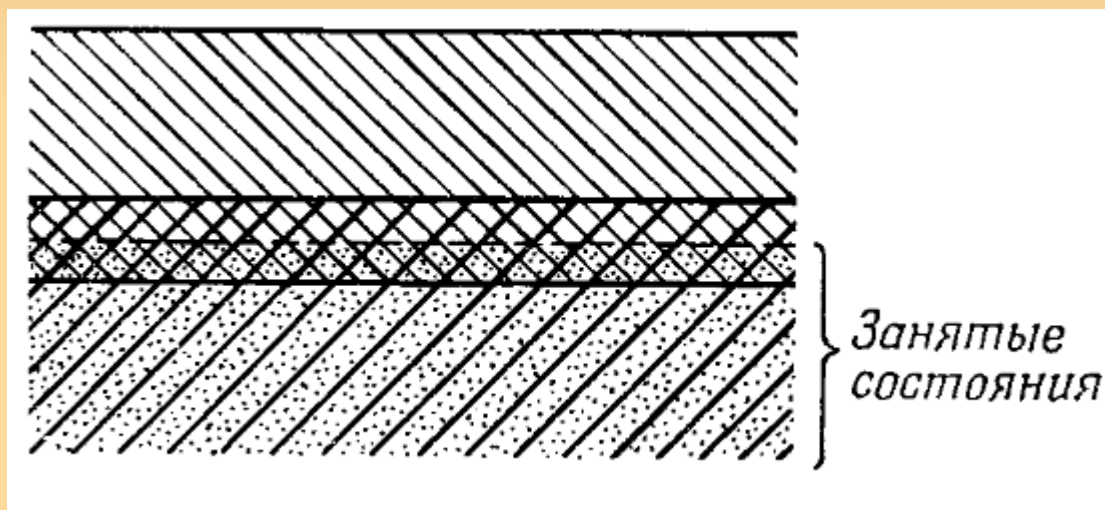
D. K. Efetov, L. Wang, C. Handschin, K. B. Efetov, J. Shuang, R. Cava, T. Taniguchi, K. Watanabe, J. Hone, C. R. Dean, P. Kim, Nature Physics (2015)

**Реализация**  
**Phys. Rev. B 93, 041303(R) (2016)**

**Зеркальное Андреевское отражение  
на границе между сверхпроводником и  
двумерным полуметаллом**

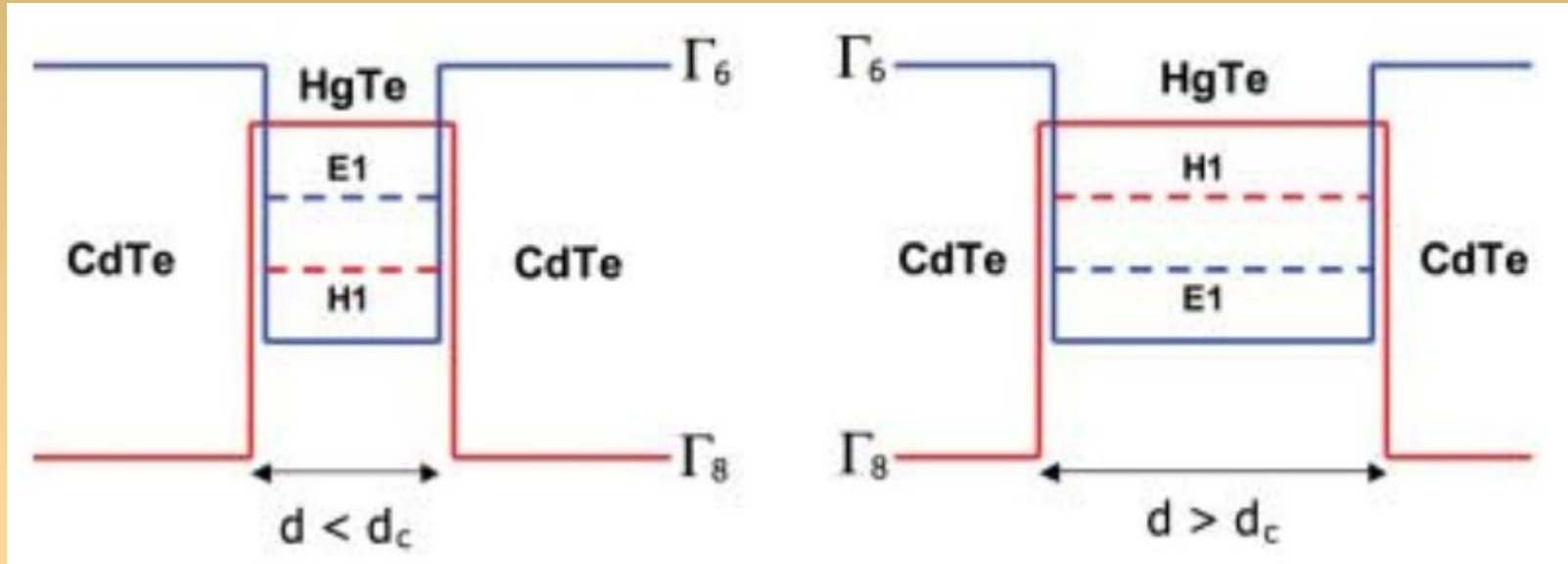
# Полуметалл

limit  $\varepsilon_F < \Delta$  - ???

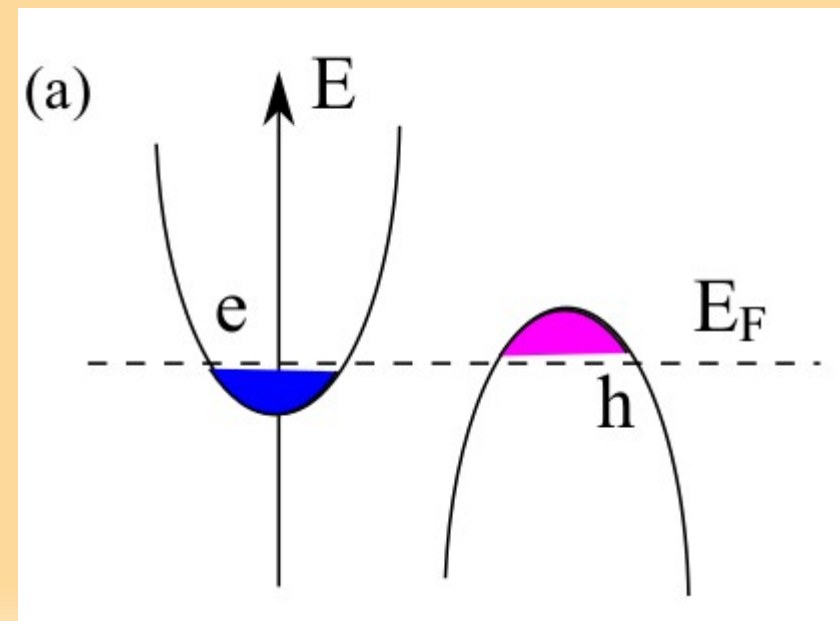


# Narrow HgTe quantum wells

## Quantum spin Hall effect

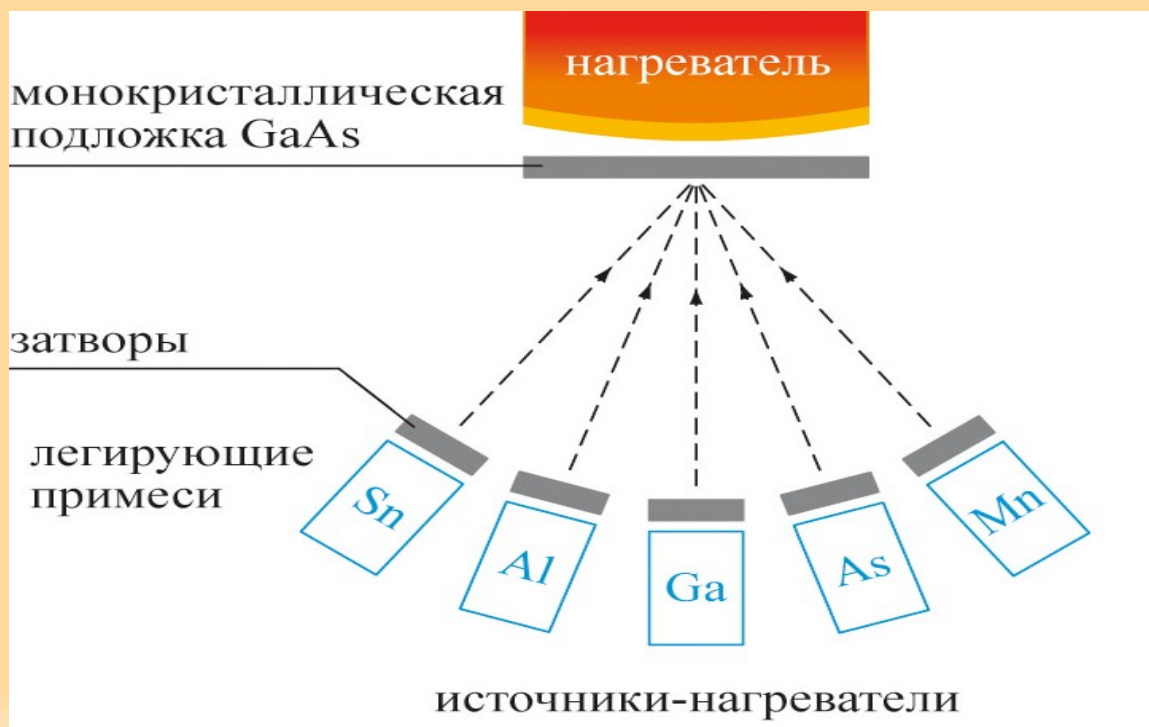
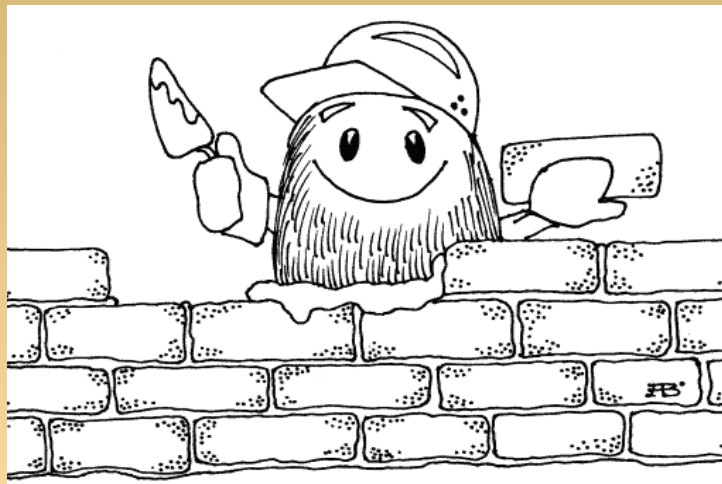


**B. A. Bernevig, S.-C. Zhang,**  
**Phys. Rev. Lett. 96, 106802 (2006)**





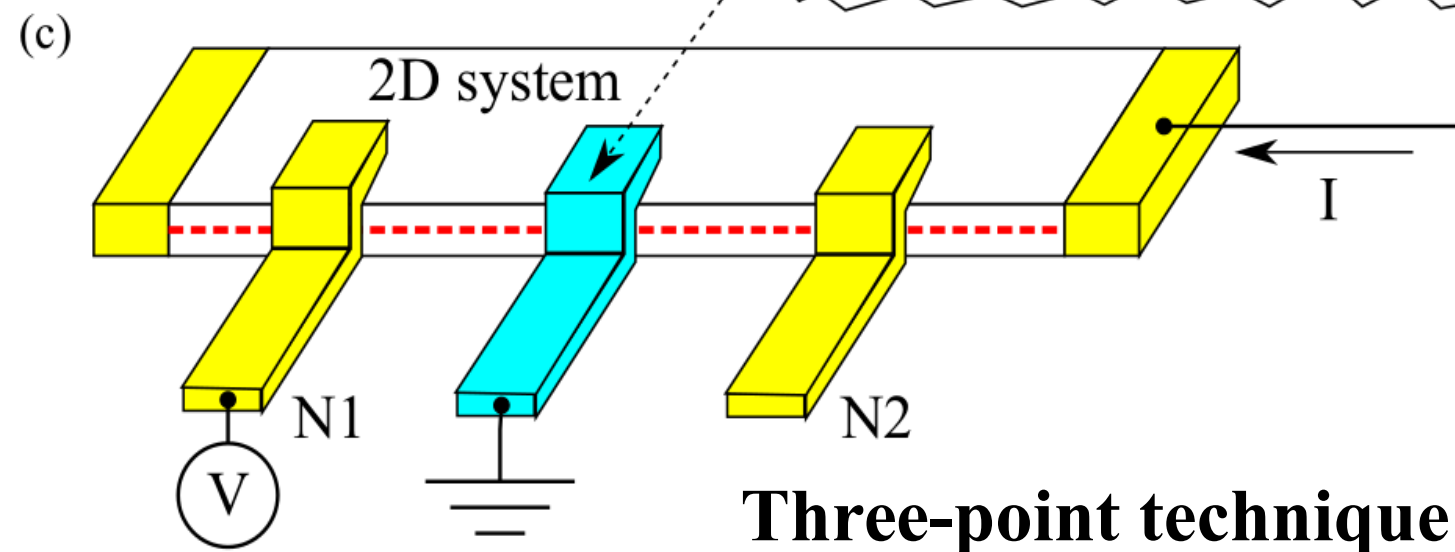
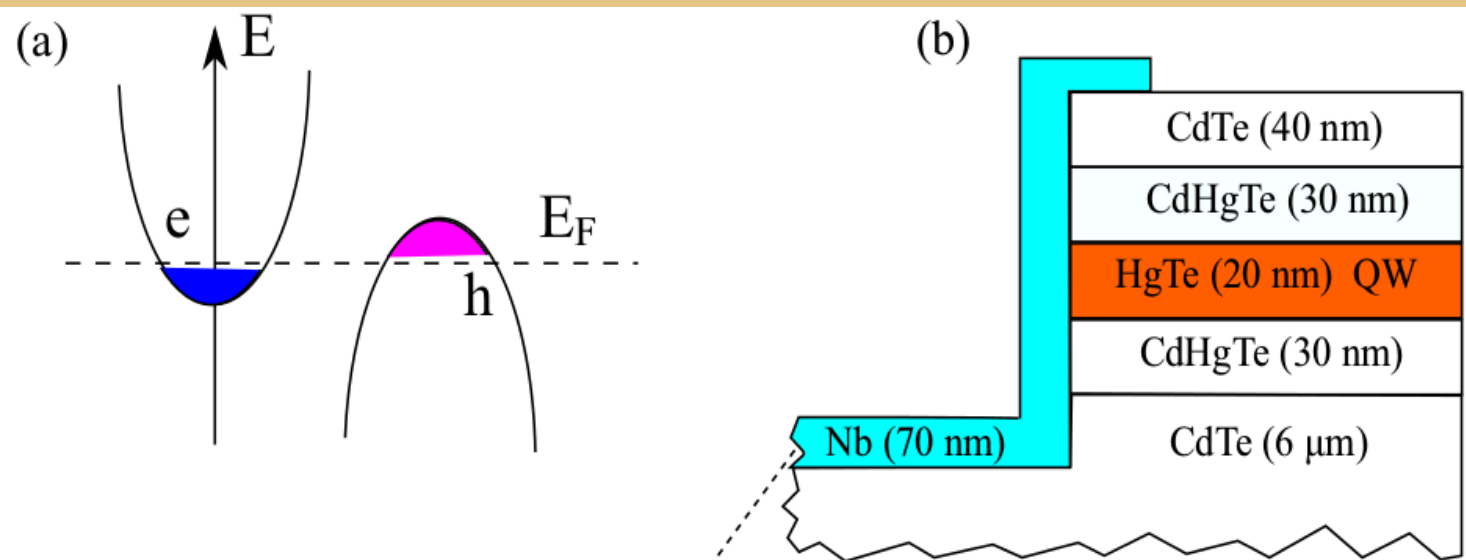
# Изготовление структур с квантовыми ямами



# Single S side contact to a 2D semimetal

Phys. Rev. B 93, 041303(R) (2016)

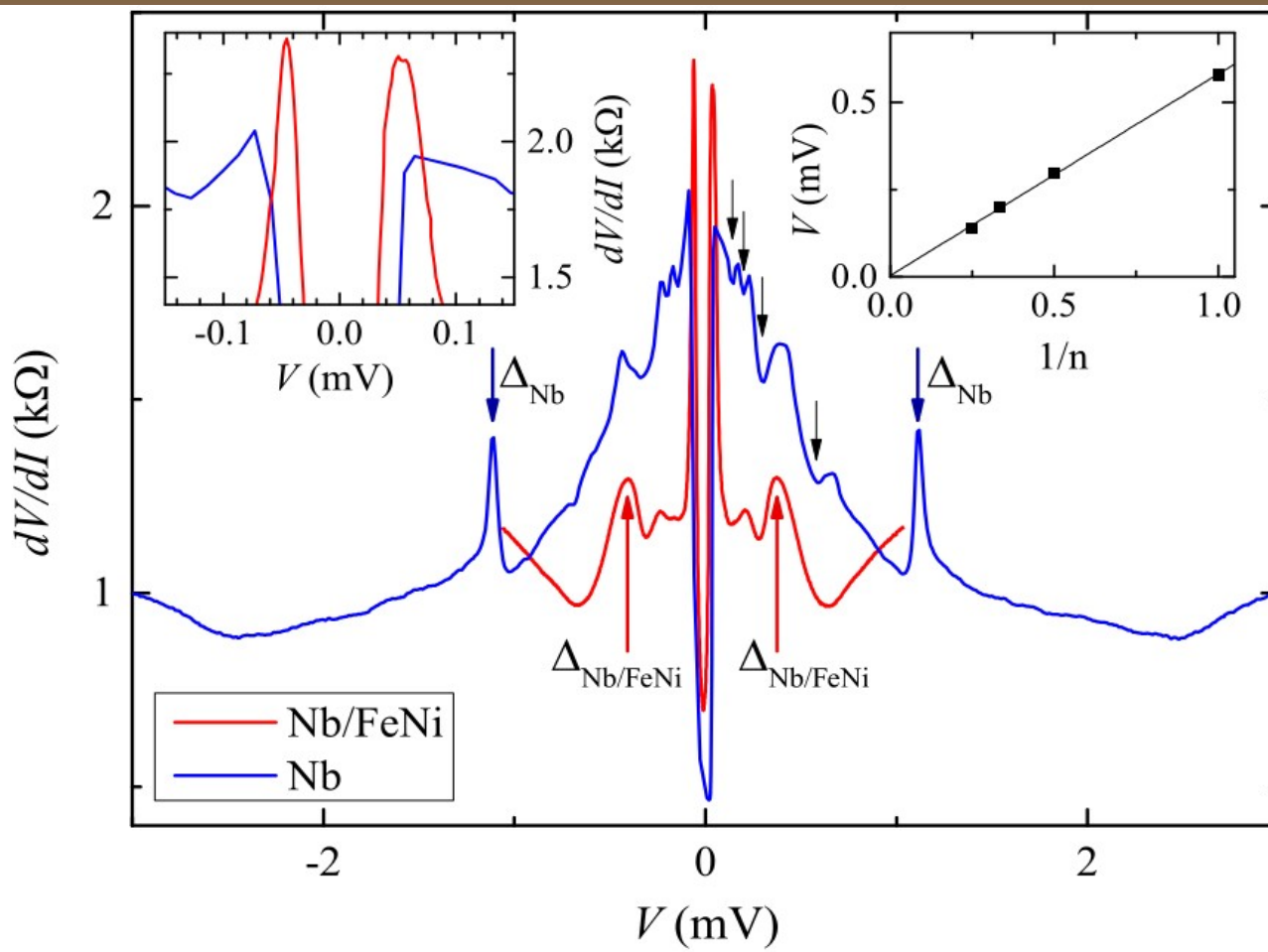
wide (  $d=20$  nm) HgTe quantum well



( $e$ :  $4 \times 10^5 \text{ cm}^2 / \text{V s}$   
at  $0.5 \times 10^{11} \text{ cm}^{-2}$ )

( $h$ :  $5 \times 10^4 \text{ cm}^2 / \text{V s}$   
at  $1 \times 10^{11} \text{ cm}^{-2}$ )

# $dV/dI(V)$ curves for a single SN interface



## Well developed Andreev curve:

(i) Every curve demonstrates a clearly defined superconducting gap ( $\pm 1.15$  mV, which is in good correspondence with the expected 9K);

(ii) the subgap resistance is undoubtedly finite, which is only possible due to Andreev reflection

$$(T=0.5 \Rightarrow Z=1 \quad (T= 1 / (1 + Z^2) )$$

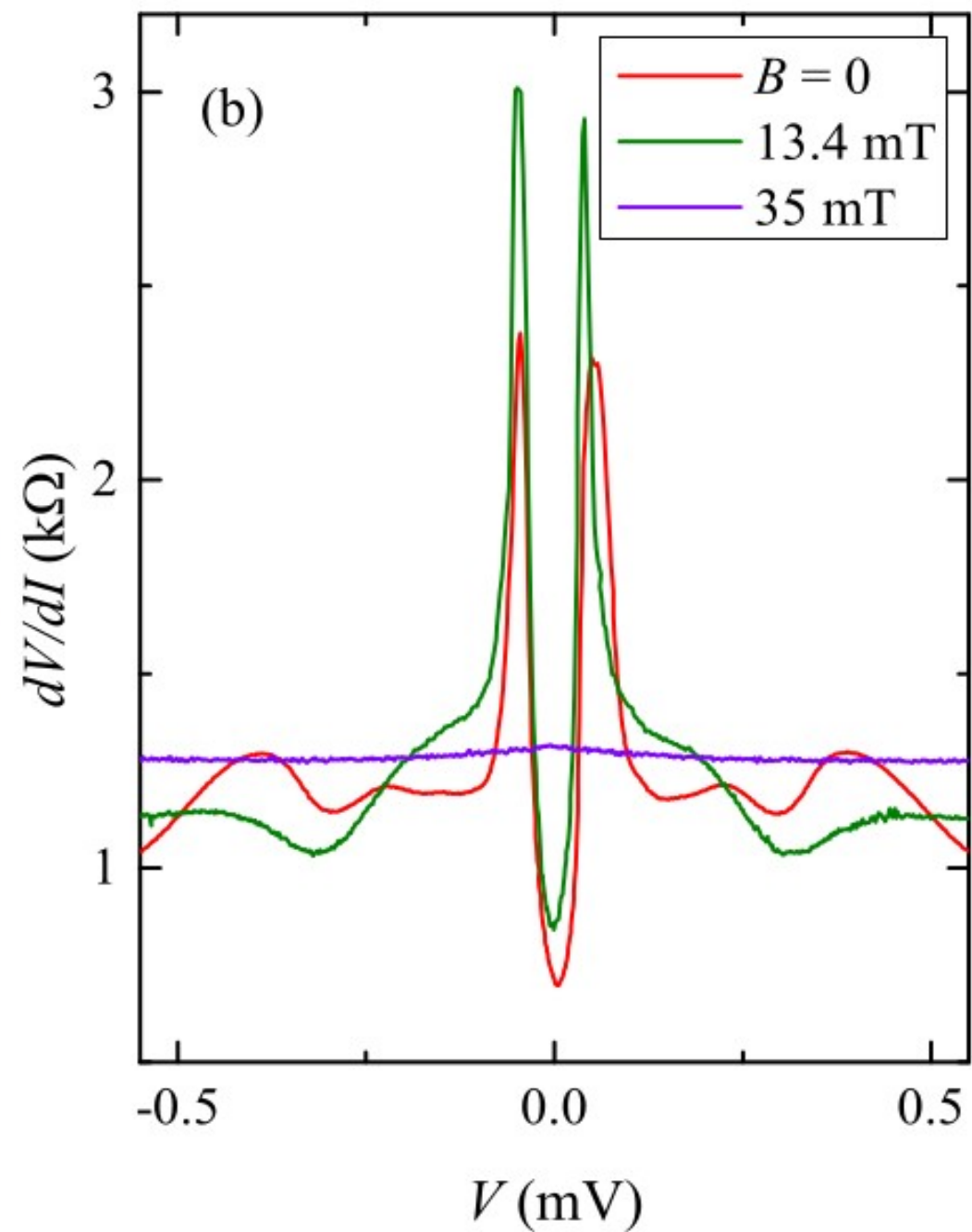
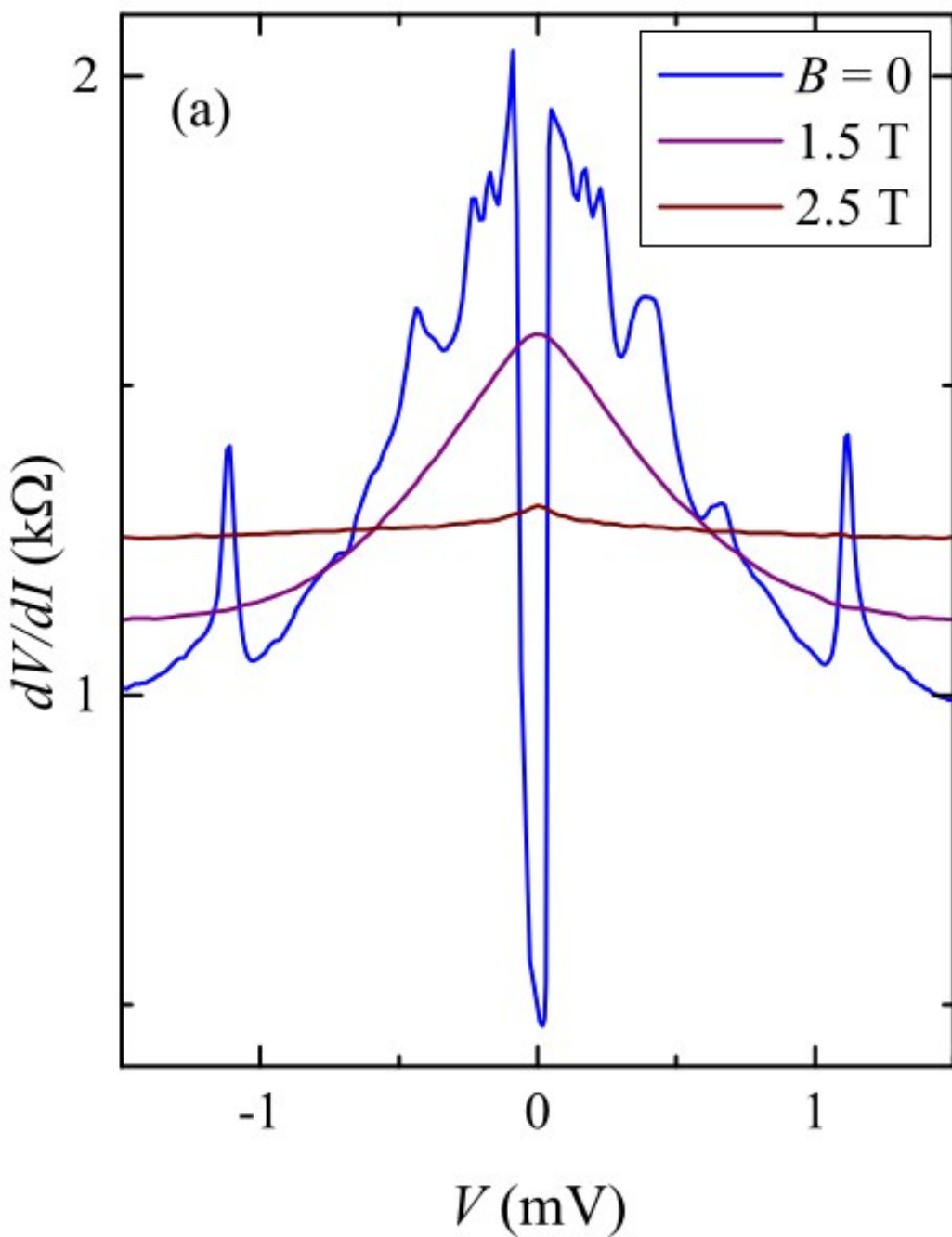
(BTK)

## The specifics of this experiment:

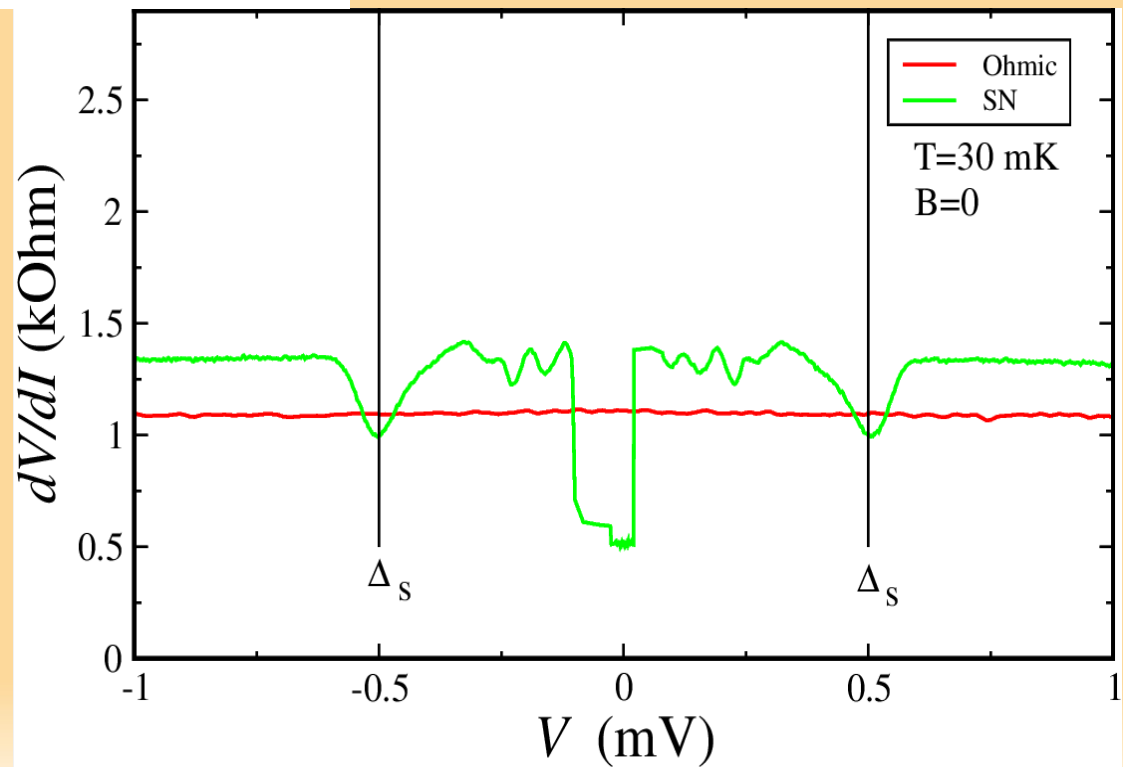
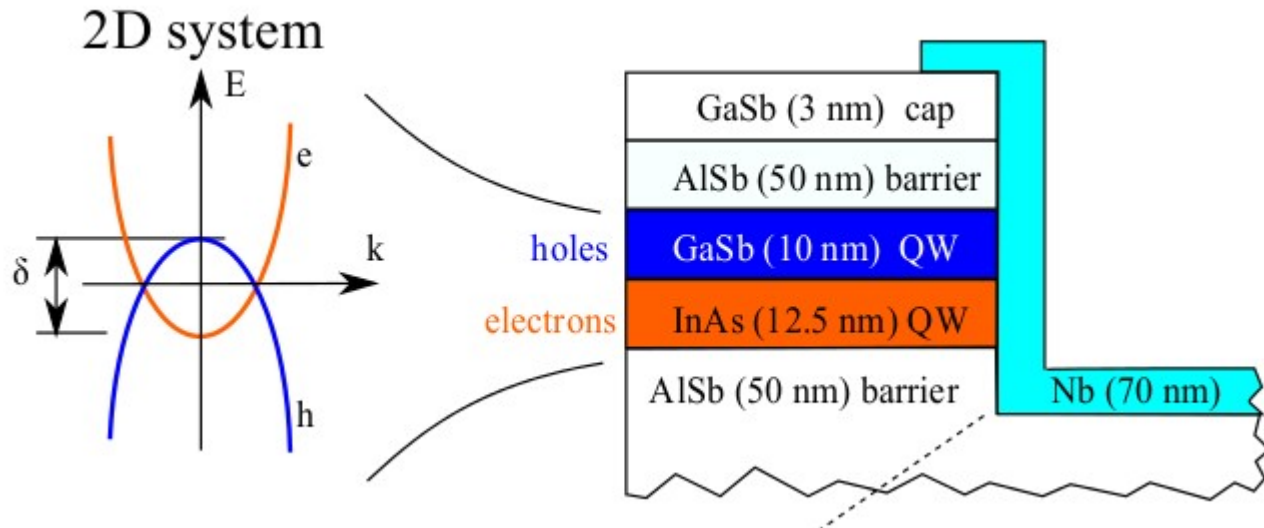
(i) Strong, twice below  $R_N$ , zero-bias differential resistance drop.

(ii) The shallow subgap resistance oscillations with  $1/n$  periodicity

# $dV/dI(V)$ curves: in-plane magnetic field dependence



# $dV/dI(V)$ curves for another semimetal (InAs/GaSb double quantum well)



# Semimetal-specific effects?

The results are independent of the superconducting material.

Similar results are obtained for different 2D semimetals.

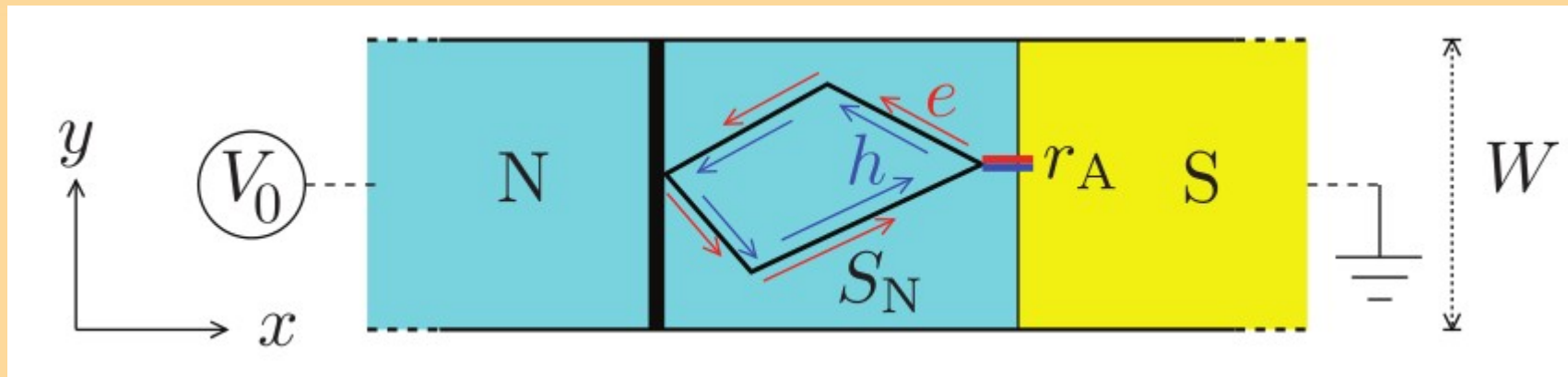
Should they be regarded as specific to a 2D semimetal in proximity with a superconductor?

# Effect of disorder?

**We cannot connect these effects with trivial disorder:**

it can only provide a small, weak antilocalization-like correction at zero bias, known as disorder-enhanced Andreev reflection (I. K. Marmorosk, C. W. J. Beenakker, and R. A. Jalabert, Phys. Rev. B 48, 2811 (1993); D. I. Pikulin, J. P. Dahlhaus, M. Wimmer, H. Schomerus, and C. W. J. Beenakker, New J. Phys. 14, 125011 (2012).).

In contrast, zero-bias resistance drops twice below the normal value in our experiment.

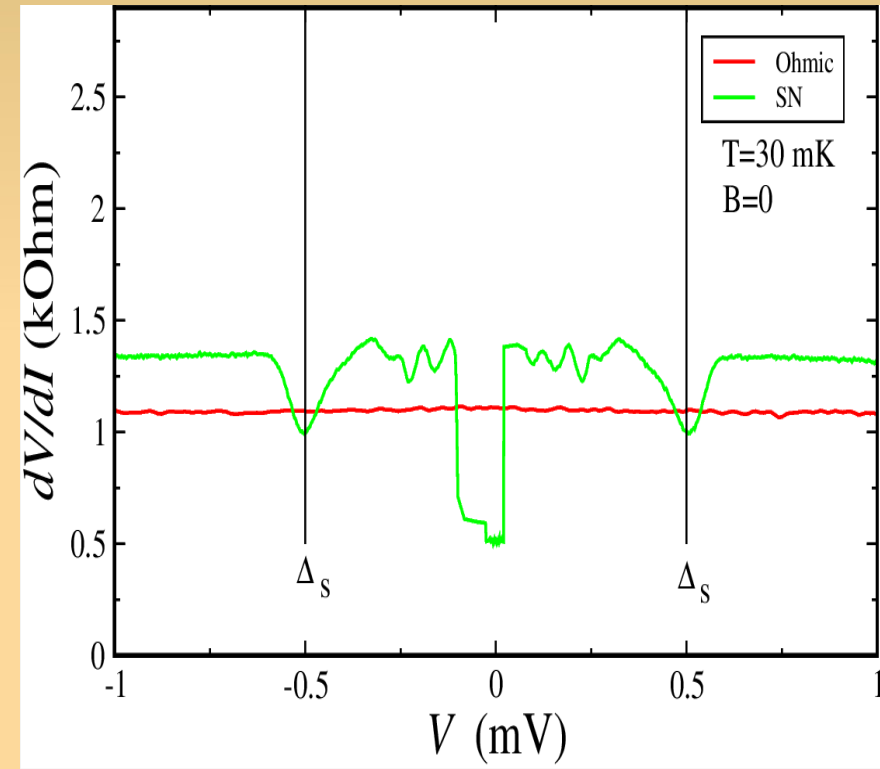
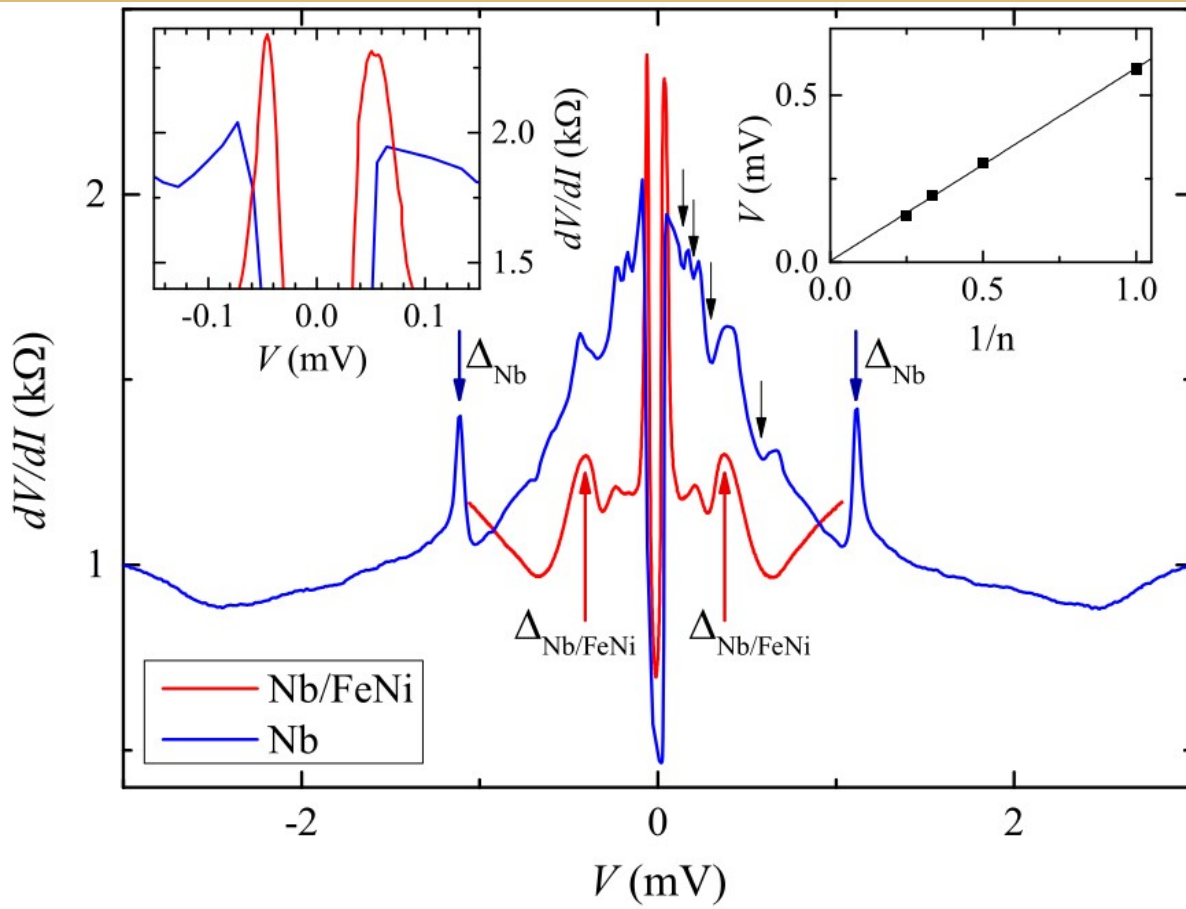


Moreover, trivial backscattering cannot provide subsequent energy increase in multiple reflections, which is responsible for the  $1/n$  periodicity:

MAR (Multiple Andreev reflection) in SNS structures

$$E_n = 2\Delta_{NbN} / n, \quad n = 1, 2, 3, \dots$$

# $dV/dI(V)$ zero-bias anomaly – different regimes of Andreev reflection



## Zero-bias region – RAR.

Its **width** is defined by the band overlap => it is independent of the particular superconductor material.

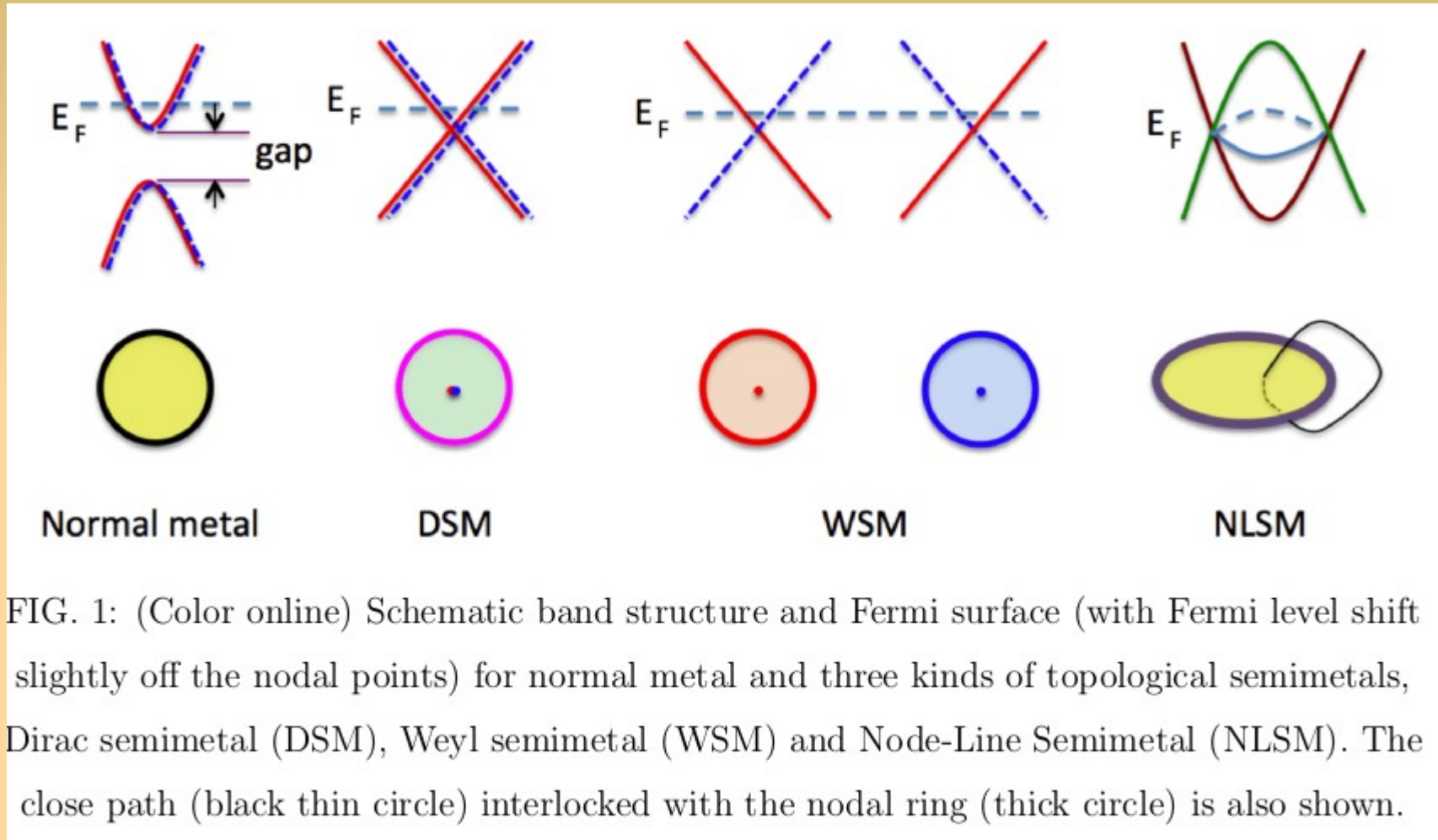
## Outside it – SAR.

The oscillations are present in SAR regime.



**Что дальше?**

# Topological semimetals



Topological Semimetals Predicted from First-principles Calculations Hongming Weng, Xi Dai, and Zhong Fang arXiv:1603.04744

# Topological semimetals

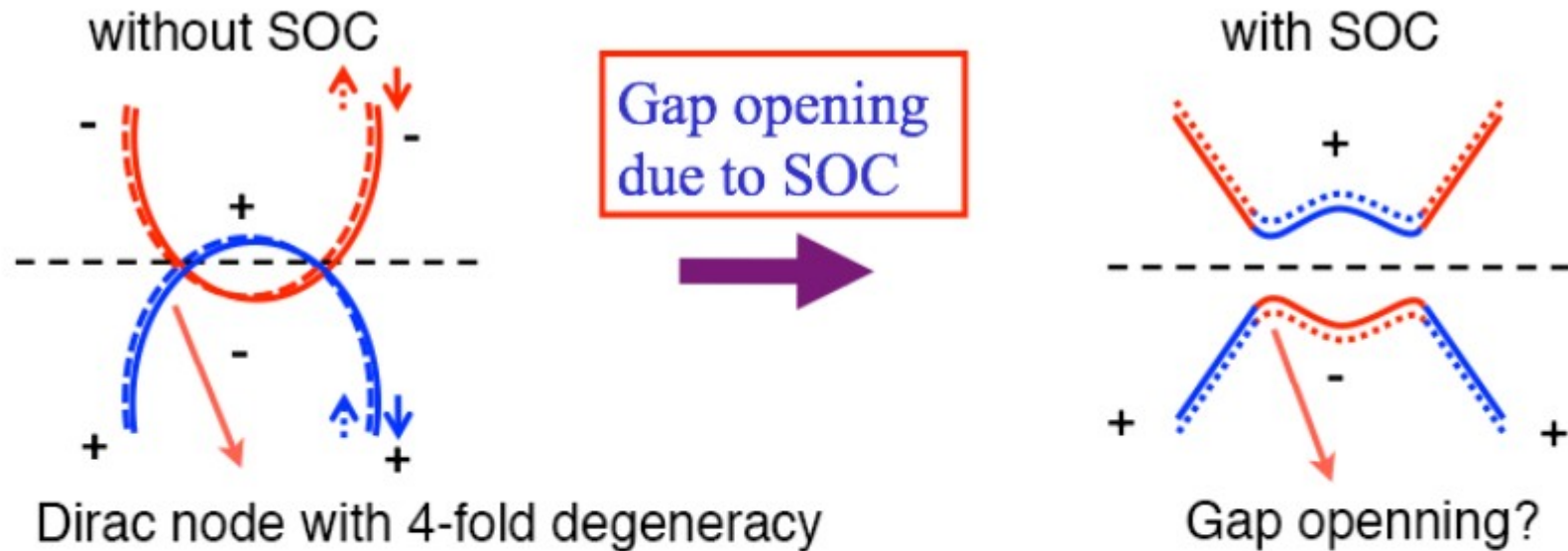


FIG. 2: (Color online) Schematic plot of band inversion mechanism. (left) The case without SOC, band inversion between two spin degenerate (dashed line for up spin, solid one for down spin) bands. + and - indicates the parity of the states at time-reversal invariant moment. (right) After including SOC, the band crossings are lifted and band gap is open.

# Благодарности

## Measurements

**A. Kononov, E.V. Deviatov**

*ISSP RAS Chernogolovka Russia*

## Samples

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*ISSP RAS Chernogolovka Russia*

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## Discussions

Ya. Fominov, A.M. Bobkov, I.V. Bobkova,

V.T. Dolgopolov, T.M. Klapwijk